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BioGSP-package *BioGSP: Biological Graph Signal Processing for Spatial Data Analysis*

Description

The BioGSP package provides a comprehensive implementation of Graph Signal Processing (GSP) methods including Spectral Graph Wavelet Transform (SGWT) for analyzing spatial patterns in biological data. This implementation is based on Hammond, Vandergheynst, and Gribonval (2011) "Wavelets on Graphs via Spectral Graph Theory".

Details

The package enables multi-scale analysis of spatial signals by:

- Building graphs from spatial coordinates using k-nearest neighbors
- Computing graph Laplacian eigendecomposition for spectral analysis
- Designing wavelets in the spectral domain using various kernel functions
- Decomposing signals into scaling and wavelet components at multiple scales
- Providing reconstruction capabilities with error analysis
- Offering comprehensive visualization and analysis tools

Main Functions

`initSGWT` Initialize SGWT object with data and parameters

`runSpecGraph` Build graph and compute eigendecomposition

`runSGWT` Perform forward and inverse SGWT transforms

`runSGCC` Calculate weighted similarity between signals

`sgwt_forward` Forward SGWT transform

`sgwt_inverse` Inverse SGWT transform

`sgwt_energy_analysis` Energy distribution analysis

`plot_sgwt_decomposition` Visualization of SGWT components

`demo_sgwt` Demonstration with synthetic data

Applications

The BioGSP package is particularly useful for:

- Spatial biology: Analyzing cell distribution patterns in tissue imaging (CODEX, Visium, etc.)
- Single-cell genomics: Spatial transcriptomics and proteomics analysis
- Neuroscience: Brain connectivity and signal analysis
- Pathology: Tumor microenvironment and tissue architecture analysis
- Developmental biology: Spatial pattern formation and cell fate mapping
- Immunology: Immune cell spatial organization and interactions

Author(s)

BioGSP Development Team

References

Hammond, D. K., Vandergheynst, P., & Gribonval, R. (2011). Wavelets on graphs via spectral graph theory. Applied and Computational Harmonic Analysis, 30(2), 129-150.

See Also

Useful links:

- https://github.com/BMEngineeR/BioGSP
- Report bugs at https://github.com/BMEngineeR/BioGSP/issues

Examples

```
# Load the package
library(BioGSP)

# Run a quick demo
demo_result <- demo_sgwt()

# Generate synthetic data
set.seed(123)
n <- 100
data <- data.frame(
  x = runif(n, 0, 10),
  y = runif(n, 0, 10),
  signal = sin(runif(n, 0, 2*pi))
)

# New workflow: Initialize -> Build Graph -> Run SGWT
SG <- initSGWT(data, signals = "signal", J = 4, kernel_type = "heat")
SG <- runSpecGraph(SG, k = 8)
SG <- runSGWT(SG)

# Analyze results
energy_analysis <- sgwt_energy_analysis(SG)
print(energy_analysis)
```

---

cal_laplacian *Calculate Graph Laplacian Matrix*

Description

Compute unnormalized, normalized, or random-walk Laplacian from an adjacency matrix.

Usage

```
cal_laplacian(W, type = c("unnormalized", "normalized", "randomwalk"))
```

Arguments

W	A square adjacency matrix (can be dense or sparse).
type	Type of Laplacian to compute: "unnormalized", "normalized", or "randomwalk".

Value

Laplacian matrix of the same class as input.

Examples

```
W <- matrix(c(0, 1, 1, 1, 0, 1, 1, 1, 0), nrow = 3)
cal_laplacian(W, type = "normalized")
```

---

checkKband *Check K-band limited property of signals*

Description

Analyze whether signals are k-band limited by comparing low-frequency and high-frequency Fourier coefficients using eigendecomposition and statistical testing. Builds graph and computes Laplacian directly from SGWT data.

Usage

```
checkKband(
  SG,
  signals = NULL,
  alpha = 0.05,
  verbose = TRUE,
  k = 25,
  laplacian_type = "normalized"
)
```

Arguments

SG	SGWT object with Data slot (from initSGWT)
signals	Character vector of signal names to analyze. If NULL, uses all signals from SG$Data$signals
alpha	Significance level for Wilcoxon test (default: 0.05)
verbose	Logical; if TRUE, print progress messages (default: TRUE)
k	Number of nearest neighbors for graph construction (default: 25)
laplacian_type	Type of Laplacian ("unnormalized", "normalized", or "randomwalk") (default: "normalized")

Value

List containing:

is_kband_limited Logical; TRUE if all signals are k-band limited

knee_point_low Integer; knee point index for low-frequency eigenvalues

knee_point_high Integer; knee point index for high-frequency eigenvalues

signal_results List with per-signal test results including p-values and Fourier coefficients

Examples

```
# Create example data
data <- data.frame(x = runif(100), y = runif(100),
                   signal1 = rnorm(100), signal2 = rnorm(100))

# Initialize SGWT object (no need to run runSpecGraph)
SG <- initSGWT(data, signals = c("signal1", "signal2"))

# Check k-band limited property
result <- checkKband(SG, signals = c("signal1", "signal2"), k = 30)
if (result$is_kband_limited) {
  cat("All signals are k-band limited")
}
```

---

codex_toy_data *Toy CODEX Spatial Cell Type Data*

Description

A synthetic dataset mimicking CODEX multiplexed imaging data for demonstrating Spectral Graph Wavelet Transform (SGWT) analysis on spatial cell type distributions. The dataset contains spatial coordinates and cell type annotations for multiple immune cell populations arranged in realistic spatial clusters.

Usage

```
data(codex_toy_data)
```

Format

A data frame with 18604 rows and 5 columns:

cellLabel Character. Unique identifier for each cell

Y_cent Numeric. Y coordinate of cell centroid (0-115 range)

X_cent Numeric. X coordinate of cell centroid (0-116 range)

Annotation5 Character. Full descriptive cell type name

ROI_num Character. Region of interest identifier ("ROI_0" through "ROI_15")

Details

The dataset contains 16 regions of interest (ROI_0 through ROI_15) with different spatial patterns and varying cell counts (945-1497 cells per ROI). Each ROI represents a distinct tissue region with unique spatial arrangements of the same cell types.

ROI Distribution:

- **ROI_0**: 952 cells
- **ROI_1**: 945 cells
- **ROI_2**: 1155 cells
- **ROI_3**: 1421 cells
- **ROI_4**: 1096 cells
- **ROI_5**: 1420 cells
- **ROI_6-ROI_15**: 958-1497 cells each

Cell types across all ROIs include:

- **BCL6- B Cell** (~3719 cells): Primary B cell population
- **CD4 T** (~4092 cells): Helper T cells - largest population
- **CD8 T** (~3346 cells): Cytotoxic T cells
- **DC** (~2233 cells): Dendritic cells
- **M1** (~1490 cells): M1 macrophages
- **CD4 Treg** (~1490 cells): Regulatory T cells
- **BCL6+ B Cell** (~931 cells): Activated B cells
- **Endothelial** (~746 cells): Vascular cells
- **M2** (~370 cells): M2 macrophages
- **Myeloid** (~186 cells): Other myeloid cells
- **Other** (~1 cells): Miscellaneous cell types

This synthetic data is designed to demonstrate:

- Spatial clustering patterns of different cell types
- Multi-scale spatial analysis using SGWT
- Cross-cell type correlation analysis
- Graph construction and eigenvalue analysis
- Wavelet decomposition of spatial signals

Source

Generated synthetically using clustered normal distributions with realistic parameters based on real CODEX data characteristics.

Examples

```
# Load the toy dataset
data(codex_toy_data)

# Examine the structure
str(codex_toy_data)
head(codex_toy_data)

# Summary of cell types
table(codex_toy_data$Annotation5)

# Summary by ROI
table(codex_toy_data$ROI_num)
table(codex_toy_data$ROI_num, codex_toy_data$Annotation5)

# Quick visualization of spatial distribution
if (requireNamespace("ggplot2", quietly = TRUE)) {
  library(ggplot2)
  ggplot(codex_toy_data, aes(x = X_cent, y = Y_cent, color = Annotation5)) +
    geom_point(size = 0.8, alpha = 0.7) +
    facet_wrap(~ROI_num, scales = "free") +
    labs(title = "Toy CODEX Spatial Cell Distribution by ROI",
         x = "X Coordinate", y = "Y Coordinate") +
    theme_minimal() +
    scale_y_reverse()
}

# Basic SGWT analysis example

# Focus on BCL6- B Cell cells in ROI_1 for SGWT analysis
bcl6nb_data <- codex_toy_data[codex_toy_data$Annotation5 == "BCL6- B Cell" &
                              codex_toy_data$ROI_num == "ROI_1", ]

# Create binned representation
library(dplyr)
binned_data <- codex_toy_data %>%
  filter(Annotation5 == "BCL6- B Cell", ROI_num == "ROI_1") %>%
  mutate(
    x_bin = cut(X_cent, breaks = 20, labels = FALSE),
    y_bin = cut(Y_cent, breaks = 20, labels = FALSE)
  ) %>%
  group_by(x_bin, y_bin) %>%
  summarise(cell_count = n(), .groups = 'drop')

# Prepare for SGWT
complete_grid <- expand.grid(x_bin = 1:20, y_bin = 1:20)
sgwt_data <- complete_grid %>%
  left_join(binned_data, by = c("x_bin", "y_bin")) %>%
  mutate(
    cell_count = ifelse(is.na(cell_count), 0, cell_count),
    x = x_bin,
    y = y_bin,
```

```
    signal = cell_count / max(cell_count, na.rm = TRUE)
  ) %>%
  select(x, y, signal)

# Apply SGWT using new workflow
SG <- initSGWT(sgwt_data, signals = "signal", J = 3, kernel_type = "heat")
SG <- runSpecGraph(SG, k = 8)
SG <- runSGWT(SG)

# View results
print(SG)
```

`compare_kernel_families` *Compare different kernel families*

Description

Visualize and compare different kernel families (both scaling and wavelet filters)

Usage

```
compare_kernel_families(
  x_range = c(0, 3),
  scale_param = 1,
  plot_results = TRUE
)
```

Arguments

`x_range`	Range of x values to evaluate (default: c(0, 3))
`scale_param`	Scale parameter for all functions (default: 1)
`plot_results`	Whether to plot the comparison (default: TRUE)

Value

Data frame with x values and kernel values for each family

Examples

```
comparison <- compare_kernel_families()
comparison <- compare_kernel_families(x_range = c(0, 5), scale_param = 1.5)
```

compute_sgwt_filters *Compute SGWT filters*

Description

Compute wavelet and scaling function coefficients in the spectral domain

Usage

```
compute_sgwt_filters(eigenvalues, scales, lmax = NULL, kernel_type = "heat")
```

Arguments

eigenvalues	Eigenvalues of the graph Laplacian
scales	Vector of scales for the wavelets
lmax	Maximum eigenvalue (optional)
kernel_type	Kernel family that defines both scaling and wavelet filters (default: "mexican_hat", options: "mexican_hat", "meyer", "heat")

Value

List of filters (scaling function + wavelets)

Examples

```
eigenvals <- c(0, 0.1, 0.5, 1.0, 1.5)
scales <- c(2, 1, 0.5)
filters <- compute_sgwt_filters(eigenvals, scales)
filters_meyer <- compute_sgwt_filters(eigenvals, scales, kernel_type = "meyer")
filters_heat <- compute_sgwt_filters(eigenvals, scales, kernel_type = "heat")
```

cosine_similarity *Calculate cosine similarity between two vectors*

Description

Calculate cosine similarity between two numeric vectors with numerical stability

Usage

```
cosine_similarity(x, y, eps = 1e-12)
```

Arguments

x	First vector
y	Second vector
eps	Small numeric for numerical stability when norms are near zero (default 1e-12)

Value

Cosine similarity value (between -1 and 1)

Examples

```
x <- c(1, 2, 3)
y <- c(2, 3, 4)
similarity <- cosine_similarity(x, y)
# With custom eps for numerical stability
similarity2 <- cosine_similarity(x, y, eps = 1e-10)
```

---

demo_sgwt *Demo function for SGWT*

Description

Demonstration function showing basic SGWT usage with synthetic data using the new workflow: initSGWT -> runSpecGraph -> runSGWT

Usage

```
demo_sgwt(verbose = TRUE)
```

Arguments

verbose	Logical; if TRUE, show progress messages and results (default: TRUE)

Value

SGWT object with complete analysis

Examples

```
SG <- demo_sgwt()
print(SG)
```

`FastDecompositionLap` *Fast eigendecomposition of Laplacian matrix*

Description

Perform fast eigendecomposition using RSpectra for large matrices

Usage

```
FastDecompositionLap(
  laplacianMat = NULL,
  k_eigen = 25,
  which = "LM",
  sigma = NULL,
  opts = list(),
  lower = TRUE,
  ...
)
```

Arguments

`laplacianMat`	Laplacian matrix
`k_eigen`	Number of eigenvalues to compute (default: 25)
`which`	Which eigenvalues to compute ("LM", "SM", etc.)
`sigma`	Shift parameter for eigenvalue computation
`opts`	Additional options for eigenvalue computation
`lower`	Whether to compute from lower end of spectrum
`...`	Additional arguments

Value

List with eigenvalues (evalues) and eigenvectors (evectors)

Examples

```
# Create a Laplacian matrix and decompose
L <- matrix(c(2, -1, -1, -1, 2, -1, -1, -1, 2), nrow = 3)
decomp <- FastDecompositionLap(L, k_eigen = 2)
```

find_knee_point *Find knee point in a curve*

Description

Simple knee point detection using the maximum curvature method

Usage

```
find_knee_point(y, sensitivity = 1)
```

Arguments

y	Numeric vector of y values
sensitivity	Sensitivity parameter (not used in this simple implementation)

Value

Index of the knee point

Examples

```
y <- c(1, 2, 3, 10, 11, 12)  # curve with a knee
knee_idx <- find_knee_point(y)
```

gft *Graph Fourier Transform*

Description

Compute the Graph Fourier Transform (GFT) of a signal using Laplacian eigenvectors.

Usage

```
gft(signal, U)
```

Arguments

signal	Input signal (vector or matrix)
U	Matrix of eigenvectors (dense matrix preferred)

Value

Transformed signal in the spectral domain (vector or matrix)

hello_sgwt *Hello function for SGWT package demonstration*

Description

Simple hello function to demonstrate package loading

Usage

```
hello_sgwt()
```

Value

Character string with greeting

Examples

```
hello_sgwt()
```

igft *Inverse Graph Fourier Transform*

Description

Compute the Inverse Graph Fourier Transform (IGFT) of spectral coefficients using Laplacian eigenvectors.

Usage

```
igft(fourier_coeffs, U)
```

Arguments

fourier_coeffs	Input Fourier coefficients (vector or matrix)
U	Matrix of eigenvectors (dense matrix preferred)

Value

Reconstructed signal in the vertex domain (vector or matrix)

Examples

```
# Create example data
data <- data.frame(x = runif(50), y = runif(50), signal = rnorm(50))
SG <- initSGWT(data, signals = "signal")
SG <- runSpecGraph(SG, k = 10)
eigenvectors <- SG$Graph$eigenvectors

# Single signal - use GFT to get Fourier coefficients
fourier_coeffs <- gft(data$signal, eigenvectors)
signal_reconstructed <- igft(fourier_coeffs, eigenvectors)

# Multiple signals (batch processing)
signals_matrix <- cbind(data$signal, data$signal * 2)
fourier_coeffs_matrix <- gft(signals_matrix, eigenvectors)
signals_reconstructed <- igft(fourier_coeffs_matrix, eigenvectors)
```

---

initSGWT *Initialize SGWT object*

Description

Build an SGWT object with Data and Parameters slots, validate inputs.

Usage

```
initSGWT(
  data.in,
  x_col = "x",
  y_col = "y",
  signals = NULL,
  scales = NULL,
  J = 5,
  scaling_factor = 2,
  kernel_type = "heat"
)
```

Arguments

data.in	Data frame containing spatial coordinates and signal data
x_col	Character string specifying the column name for X coordinates (default: "x")
y_col	Character string specifying the column name for Y coordinates (default: "y")
signals	Character vector of signal column names to analyze. If NULL, all non-coordinate columns are used.
scales	Vector of scales for the wavelets. If NULL, scales are auto-generated.
J	Number of scales to generate if scales is NULL (default: 5)
scaling_factor	Scaling factor between consecutive scales (default: 2)
kernel_type	Kernel family ("mexican_hat", "meyer", or "heat") (default: "heat")

Value

SGWT object with Data and Parameters slots initialized

Examples

```
# Initialize SGWT object
data <- data.frame(x = runif(100), y = runif(100),
                   signal1 = rnorm(100), signal2 = rnorm(100))
SG <- initSGWT(data, signals = c("signal1", "signal2"))
```

---

plot_FM *Plot Fourier modes (eigenvectors) from SGWT object*

Description

Plot low-frequency and high-frequency Fourier modes (eigenvectors) from the graph Laplacian eigendecomposition in an SGWT object

Usage

```
plot_FM(SG, mode_type = "both", n_modes = 6, ncol = 3, point_size = 1.5)
```

Arguments

SG	SGWT object with Graph slot computed (from runSpecGraph)
mode_type	Type of modes to plot: "low", "high", or "both" (default: "both")
n_modes	Number of modes to plot for each type (default: 6)
ncol	Number of columns in plot layout (default: 3)
point_size	Size of points in the plot (default: 1.5)

Value

Combined plot of Fourier modes

Examples

```
# Create example data
data <- data.frame(x = runif(100), y = runif(100), signal = rnorm(100))

# Plot both low and high frequency modes
SG <- initSGWT(data, signals = "signal")
SG <- runSpecGraph(SG, k = 15)
plot_FM(SG, mode_type = "both", n_modes = 4)

# Plot only low frequency modes
plot_FM(SG, mode_type = "low", n_modes = 8)
```

plot_sgwt_decomposition *Plot SGWT decomposition results*

Description

Visualize SGWT decomposition components including original signal, scaling function, wavelet coefficients, and reconstructed signal

Usage

```
plot_sgwt_decomposition(SG, signal_name = NULL, plot_scales = NULL, ncol = 3)
```

Arguments

SG	SGWT object with Forward and Inverse results computed
signal_name	Name of signal to plot (default: first signal)
plot_scales	Which wavelet scales to plot (default: first 4)
ncol	Number of columns in the plot layout (default: 3)

Value

ggplot object with combined plots

Examples

```
# Create and analyze example data
data <- data.frame(x = runif(100), y = runif(100), signal1 = rnorm(100))
SG <- initSGWT(data, signals = "signal1")
SG <- runSpecGraph(SG, k = 15)
SG <- runSGWT(SG)

# Plot decomposition
plots <- plot_sgwt_decomposition(SG, signal_name = "signal1")
print(plots)
```

print.SGWT *Print method for SGWT objects*

Description

Print method for SGWT objects

Usage

```
## S3 method for class 'SGWT'
print(x, ...)
```

Arguments

x	SGWT object to print
...	Additional arguments passed to print methods

Value

Invisibly returns the input SGWT object. Called for side effects (prints object summary to console).

---

runSGCC *Run SGCC weighted similarity analysis in Fourier domain*

Description

Calculate energy-normalized weighted similarity between two signals using Fourier domain coefficients directly (no vertex domain reconstruction). Excludes DC component and uses energy-based weighting consistent with Parseval's theorem.

Usage

```
runSGCC(
  signal1,
  signal2,
  SG = NULL,
  eps = 1e-12,
  validate = TRUE,
  return_parts = TRUE,
  low_only = FALSE
)
```

Arguments

signal1	Either a signal name (character) for SG object, or SGWT Forward result, or SGWT object
signal2	Either a signal name (character) for SG object, or SGWT Forward result, or SGWT object
SG	SGWT object (required if signal1/signal2 are signal names)
eps	Small numeric for numerical stability (default: 1e-12)
validate	Logical; if TRUE, check consistency (default: TRUE)
return_parts	Logical; if TRUE, return detailed components (default: TRUE)
low_only	Logical; if TRUE, compute only low-frequency similarity (default: FALSE)

Value

Similarity analysis results computed in Fourier domain

Examples

```
# Create example data and compute SGWT
data <- data.frame(x = runif(100), y = runif(100),
                   signal1 = rnorm(100), signal2 = rnorm(100))
SG <- initSGWT(data, signals = c("signal1", "signal2"))
SG <- runSpecGraph(SG, k = 15)
SG <- runSGWT(SG)

# Between two signals in same SGWT object
similarity <- runSGCC("signal1", "signal2", SG = SG)
print(similarity)

# Between two SGWT objects
data2 <- data.frame(x = runif(100), y = runif(100), signal = rnorm(100))
SG2 <- initSGWT(data2, signals = "signal")
SG2 <- runSpecGraph(SG2, k = 15)
SG2 <- runSGWT(SG2)

similarity2 <- runSGCC(SG, SG2)
print(similarity2)
```

---

runSGWT *Run SGWT forward and inverse transforms for all signals*

Description

Perform SGWT analysis on all signals in the SGWT object. Uses batch processing for multiple signals when possible for efficiency. Assumes Graph slot is populated by runSpecGraph().

Usage

```
runSGWT(SG, use_batch = TRUE, verbose = TRUE)
```

Arguments

SG	SGWT object with Graph slot populated
use_batch	Whether to use batch processing for multiple signals (default: TRUE)
verbose	Whether to print progress messages (default: TRUE)

Value

Updated SGWT object with Forward and Inverse slots populated

Examples

```
# Create example data
data <- data.frame(x = runif(100), y = runif(100), signal = rnorm(100))
SG <- initSGWT(data, signals = "signal")
SG <- runSpecGraph(SG, k = 15)

# Uses batch processing by default
SG <- runSGWT(SG)

# Or force individual processing
SG2 <- initSGWT(data, signals = "signal")
SG2 <- runSpecGraph(SG2, k = 15)
SG2 <- runSGWT(SG2, use_batch = FALSE)
```

---

runSpecGraph *Build spectral graph for SGWT object*

Description

Generate Graph slot information including adjacency matrix, Laplacian matrix, eigenvalues, and eigenvectors.

Usage

```
runSpecGraph(
  SG,
  k = 25,
  laplacian_type = "normalized",
  length_eigenvalue = NULL,
  verbose = TRUE
)
```

Arguments

SG	SGWT object from initSGWT()
k	Number of nearest neighbors for graph construction (default: 25)
laplacian_type	Type of graph Laplacian ("unnormalized", "normalized", or "randomwalk") (default: "normalized")
length_eigenvalue	Number of eigenvalues/eigenvectors to compute (default: NULL, uses full length)
verbose	Whether to print progress messages (default: TRUE)

Value

Updated SGWT object with Graph slot populated

Examples

```
# Create example data
data <- data.frame(x = runif(100), y = runif(100), signal = rnorm(100))
SG <- initSGWT(data, signals = "signal")

# Uses full length by default
SG <- runSpecGraph(SG, k = 30, laplacian_type = "normalized")

# Or specify custom length
SG2 <- initSGWT(data, signals = "signal")
SG2 <- runSpecGraph(SG2, k = 30, laplacian_type = "normalized",
                    length_eigenvalue = 30)
```

---

sgwt_auto_scales *Generate automatic scales for SGWT*

Description

Generate logarithmically spaced scales for SGWT

Usage

```
sgwt_auto_scales(lmax, J = 5, scaling_factor = 2)
```

Arguments

lmax	Maximum eigenvalue
J	Number of scales
scaling_factor	Scaling factor between consecutive scales

Value

Vector of scales

Examples

```
scales <- sgwt_auto_scales(lmax = 2.0, J = 5, scaling_factor = 2)
```

sgwt_energy_analysis *Analyze SGWT energy distribution across scales in Fourier domain*

Description

Calculate and analyze energy distribution across different scales using Fourier domain coefficients directly (consistent with Parseval's theorem). Excludes DC component for more accurate energy analysis.

Usage

```
sgwt_energy_analysis(SG, signal_name = NULL)
```

Arguments

SG	SGWT object with Forward results computed
signal_name	Name of signal to analyze (default: first signal)

Value

Data frame with energy analysis results computed in Fourier domain

Examples

```
# Create and analyze example data
data <- data.frame(x = runif(100), y = runif(100), signal1 = rnorm(100))
SG <- initSGWT(data, signals = "signal1")
SG <- runSpecGraph(SG, k = 15)
SG <- runSGWT(SG)

# Analyze energy distribution
energy_analysis <- sgwt_energy_analysis(SG, signal_name = "signal1")
print(energy_analysis)
```

sgwt_forward *Forward SGWT transform (single or batch)*

Description

Transform signal(s) to spectral domain and apply SGWT filters. Handles both single signals (vector) and multiple signals (matrix) efficiently. Stores original and filtered Fourier coefficients for analysis.

Usage

```
sgwt_forward(
  signal,
  eigenvectors,
  eigenvalues,
  scales,
  lmax = NULL,
  kernel_type = "heat"
)
```

Arguments

signal	Input signal vector OR matrix where each column is a signal (n_vertices x n_signals)
eigenvectors	Eigenvectors of the graph Laplacian
eigenvalues	Eigenvalues of the graph Laplacian
scales	Vector of scales for the wavelets
lmax	Maximum eigenvalue (optional)
kernel_type	Kernel family that defines both scaling and wavelet filters (default: "heat")

Value

List containing:

fourier_coefficients List with original and filtered Fourier coefficients

filters Filter bank used

Examples

```
# Create example data and compute graph
data <- data.frame(x = runif(50), y = runif(50), signal = rnorm(50))
SG <- initSGWT(data, signals = "signal", J = 3)
SG <- runSpecGraph(SG, k = 10)
eigenvectors <- SG$Graph$eigenvectors
eigenvalues <- SG$Graph$eigenvalues
scales <- SG$Parameters$scales

# Single signal
signal <- data$signal
result <- sgwt_forward(signal, eigenvectors, eigenvalues, scales)

# Multiple signals (batch processing)
signals_matrix <- cbind(data$signal, data$signal * 2, data$signal * 0.5)
result <- sgwt_forward(signals_matrix, eigenvectors, eigenvalues, scales)
```

sgwt_get_kernels *Get a unified kernel family (low-pass and band-pass) by kernel_type*

Description

Returns a pair of functions implementing the scaling (low-pass) and wavelet (band-pass) kernels for a given kernel family. This enforces consistency: a single kernel_type defines both filters.

Usage

```
sgwt_get_kernels(kernel_type = "heat")
```

Arguments

kernel_type	Kernel family name ("mexican_hat", "meyer", or "heat")

Value

A list with two functions: list(scaling = function(x, scale_param), wavelet = function(x, scale_param))

sgwt_inverse *Inverse SGWT transform (single or batch)*

Description

Reconstruct signal(s) from filtered Fourier coefficients using inverse GFT. Handles both single signals and multiple signals efficiently. Returns detailed inverse transform results including low-pass, band-pass approximations, reconstructed signal(s), and reconstruction error(s).

Usage

```
sgwt_inverse(sgwt_decomp, eigenvectors, original_signal = NULL)
```

Arguments

sgwt_decomp	SGWT decomposition object from sgwt_forward
eigenvectors	Eigenvectors of the graph Laplacian (for inverse GFT)
original_signal	Original signal vector OR matrix (n_vertices x n_signals) for error calculation (optional)

Value

List containing:

vertex_approximations Named list with inverse-transformed signals in vertex domain:

- `low_pass`: Low-pass (scaling) approximation
- `wavelet_1`, `wavelet_2`, etc.: Band-pass (wavelet) approximations by scale

reconstructed_signal Full reconstructed signal (vector or matrix)

reconstruction_error RMSE (scalar for single signal, vector for multiple signals)

Examples

```
# Create example data and perform forward transform
data <- data.frame(x = runif(50), y = runif(50), signal = rnorm(50))
SG <- initSGWT(data, signals = "signal", J = 3)
SG <- runSpecGraph(SG, k = 10)
eigenvectors <- SG$Graph$eigenvectors
eigenvalues <- SG$Graph$eigenvalues
scales <- SG$Parameters$scales

# Single signal - forward transform first
original_signal <- data$signal
sgwt_decomp <- sgwt_forward(original_signal, eigenvectors, eigenvalues, scales)
inverse_result <- sgwt_inverse(sgwt_decomp, eigenvectors, original_signal)

# Multiple signals (batch processing)
original_signals_matrix <- cbind(data$signal, data$signal * 2)
sgwt_decomp <- sgwt_forward(original_signals_matrix, eigenvectors, eigenvalues, scales)
inverse_result <- sgwt_inverse(sgwt_decomp, eigenvectors, original_signals_matrix)
```

`simulate_checkerboard` *Simulate checkerboard pattern*

Description

Generate a checkerboard pattern with alternating signals

Usage

```
simulate_checkerboard(grid_size = 8, tile_size = 1)
```

Arguments

`grid_size`	Number of tiles per row/column (default: 8)
`tile_size`	Resolution of each tile in pixels per side (default: 1)

Value

Data frame with X, Y coordinates and signal_1, signal_2 patterns

Examples

```
# Generate 8x8 checkerboard with 10x10 pixel tiles
df <- simulate_checkerboard(grid_size = 8, tile_size = 10)
p <- visualize_checkerboard(df)
print(p)
```

---

simulate_moving_circles

Simulate Moving Circles Pattern

Description

Generate patterns of two circles moving toward each other horizontally. Creates mutually exclusive signals where overlapping pixels are assigned to signal_1 (circle 1). The circles start at fixed horizontal distances from the midline and move toward the center.

Usage

```
simulate_moving_circles(
  grid_size = 60,
  radius_seq = 6:14,
  n_steps = 10,
  center_distance = 30,
  radius2_factor = 1.5,
  seed = NULL,
  verbose = TRUE
)
```

Arguments

grid_size	Size of the spatial grid (default: 60)
radius_seq	Vector of radii for circle 1 (default: 6:14)
n_steps	Number of movement steps (default: 10)
center_distance	Initial horizontal distance from midline for both centers (default: 30)
radius2_factor	Circle 2 radius = radius_seq * radius2_factor (default: 1.5)
seed	Random seed for reproducibility (default: 123)
verbose	Logical; if TRUE, show progress bar and messages (default: TRUE)

Value

List of data frames, each containing X, Y coordinates and signal_1, signal_2 binary signals

Examples

```
# Generate moving circles patterns with default parameters
patterns <- simulate_moving_circles()

# Custom parameters
patterns <- simulate_moving_circles(
  grid_size = 80,
  radius_seq = c(8, 12, 16),
  n_steps = 8,
  center_distance = 35,
  radius2_factor = 1.2
)
```

---

simulate_multiscale *Simulate Multi-center Multi-scale Concentric Ring Patterns*

Description

Generate multi-center, multi-scale concentric ring simulation data. Creates patterns with inner circles and outer rings where the outer radius shrinks from a fixed starting point to a factor of the inner radius across multiple steps.

Usage

```
simulate_multiscale(
  grid_size = 60,
  Ra_seq = seq(2.5, 20, by = 2.5),
  n_steps = 10,
  n_centers = 1,
  outer_start = 40,
  outer_end_factor = 1.2,
  seed = NULL,
  verbose = TRUE
)
```

Arguments

grid_size	Size of the spatial grid (default: 60)
Ra_seq	Vector of inner circle radii (default: seq(2.5, 20, by = 2.5))
n_steps	Number of outer radius shrinkage steps (default: 10)
n_centers	Number of circle centers (default: 1)
outer_start	Fixed starting outer radius (default: 40)

outer_end_factor	Outer radius shrinks to this factor * Ra (default: 1.2)
seed	Random seed for reproducible center placement (default: 123)
verbose	Logical; if TRUE, show progress bar and messages (default: TRUE)

Value

List of data frames, each containing X, Y coordinates and signal_1, signal_2 binary signals

Examples

```
# Generate multi-center patterns with default parameters
patterns <- simulate_multiscale()

# Custom parameters
patterns <- simulate_multiscale(
  grid_size = 80,
  Ra_seq = seq(5, 25, by = 5),
  n_steps = 8,
  n_centers = 2,
  outer_start = 50
)
```

---

simulate_multiscale_overlap

Simulate Multiple Center Patterns with Fixed Centers

Description

Generate spatial patterns with multiple circular centers at fixed positions. Similar to simulate_multiscale but with centers placed at fixed locations for reproducible pattern generation. Creates concentric circle patterns with inner circle A and outer ring B at various radius combinations.

Usage

```
simulate_multiscale_overlap(
  grid_size = 60,
  n_centers = 3,
  Ra_seq = c(10, 5, 1),
  Rb_seq = c(10, 5, 1),
  seed = NULL,
  verbose = TRUE
)
```

Arguments

grid_size	Size of the spatial grid (default: 60)
n_centers	Number of pattern centers to generate. If 1, center is placed at grid center. If > 1, centers are randomly placed but fixed by seed (default: 3)
Ra_seq	Vector of inner circle radii (default: c(10, 5, 1))
Rb_seq	Vector of outer ring radii (default: c(10, 5, 1))
seed	Random seed for reproducible center placement (default: 123)
verbose	Logical; if TRUE, show progress bar and messages (default: TRUE)

Value

List of data frames, each containing X, Y coordinates and signal_1, signal_2 binary signals

Examples

```
# Generate multi-center patterns with fixed centers
patterns <- simulate_multiscale_overlap()

# Single center at grid center
patterns_single <- simulate_multiscale_overlap(n_centers = 1)

# Custom parameters with multiple centers
Ra_seq <- seq(from = 10, to = 3, length.out = 4)
Rb_seq <- seq(from = 15, to = 2, length.out = 4)
patterns <- simulate_multiscale_overlap(
  Ra_seq = Ra_seq,
  Rb_seq = Rb_seq,
  n_centers = 2,
  seed = 456
)
```

---

simulate_stripe_patterns

Simulate Stripe Patterns

Description

Generate stripe patterns with two parallel stripes separated by a gap. Creates rotatable stripe patterns with configurable gap, width, and rotation angle.

Usage

```
simulate_stripe_patterns(
  grid_size = 100,
  gap_seq = c(10),
  width_seq = c(5),
  theta_seq = c(0),
  eps = 1e-09,
  verbose = TRUE
)
```

Arguments

grid_size	Size of the spatial grid (default: 100)
gap_seq	Vector of gap distances between stripe centers (default: c(10))
width_seq	Vector of stripe widths (default: c(5))
theta_seq	Vector of rotation angles in degrees (default: c(0))
eps	Small numeric value for open boundary conditions to avoid overlap at stripe edges (default: 1e-9)
verbose	Logical; if TRUE, show progress messages (default: TRUE)

Value

List of data frames, each containing X, Y coordinates and signal_1, signal_2 binary signals

Examples

```
# Generate stripe patterns with default parameters
patterns <- simulate_stripe_patterns()

# Custom parameters
patterns <- simulate_stripe_patterns(
  grid_size = 80,
  gap_seq = c(10, 20),
  width_seq = c(5, 10, 20),
  theta_seq = c(0, 30, 60),
  eps = 1e-9,
  verbose = TRUE
)
```

---

visualize_checkerboard

Visualize checkerboard pattern

Description

Create a visualization of checkerboard pattern data

Usage

```
visualize_checkerboard(df, color1 = "black", color2 = "white")
```

Arguments

df	Data frame with X, Y coordinates and signal_1, signal_2 columns
color1	Color for signal_1 tiles (default: "black")
color2	Color for signal_2 tiles (default: "white")

Value

ggplot object showing the checkerboard pattern

Examples

```
df <- simulate_checkerboard(grid_size = 6, tile_size = 5)
p <- visualize_checkerboard(df, color1 = "darkblue", color2 = "lightgray")
print(p)
```

---

visualize_moving_circles

Visualize Moving Circles Pattern

Description

Visualize the simulated moving circles patterns from simulate_moving_circles

Usage

```
visualize_moving_circles(
  sim_data,
  bg_color = "grey90",
  signal1_color = "#16964a",
  signal2_color = "#2958a8",
  show_subtitle = TRUE,
  sort_order = c("ascending", "descending"),
  panel_spacing = 0.1,
  title_size = 12
)
```

Arguments

sim_data	Output from simulate_moving_circles function
bg_color	Background color for plots (default: "grey90")
signal1_color	Color for signal 1 (default: "#16964a")
signal2_color	Color for signal 2 (default: "#2958a8")
show_subtitle	Logical; if TRUE (default), show parameter values in facet labels
sort_order	Order for sorting ("ascending" or "descending", default: "ascending")
panel_spacing	Control spacing between panels in lines (default: 0.1)
title_size	Size of title text (default: 12)

Value

ggplot object with faceted visualization

Examples

```
# Generate and visualize patterns
sim_data <- simulate_moving_circles(
  radius_seq = 6:14,
  n_steps = 10
)
plot_grid <- visualize_moving_circles(sim_data)
print(plot_grid)
```

---

visualize_multiscale *Visualize Multi-center Multi-scale Concentric Ring Patterns*

Description

Visualize the simulated concentric ring patterns from simulate_multiscale

Usage

```
visualize_multiscale(
  sim_data,
  Ra_seq,
  n_steps,
  bg_color = "grey90",
  signal1_color = "#16964a",
  signal2_color = "#2958a8",
  show_subtitle = TRUE,
  sort_order = c("ascending", "descending"),
  panel_spacing = 0.1,
  title_size = 12
)
```

Arguments

sim_data	Output from simulate_multiscale function
Ra_seq	Vector of Ra values used in simulation
n_steps	Number of steps used in simulation
bg_color	Background color for plots (default: "grey90")
signal1_color	Color for signal 1 (default: "#16964a")
signal2_color	Color for signal 2 (default: "#2958a8")
show_subtitle	Logical; if TRUE (default), show parameter values in facet labels
sort_order	Order for sorting ("ascending" or "descending", default: "ascending")
panel_spacing	Control spacing between panels in lines (default: 0.1)
title_size	Size of title text (default: 12)

Value

ggplot object with faceted visualization

Examples

```
# Generate and visualize patterns
sim_data <- simulate_multiscale(
  Ra_seq = seq(2.5, 20, by = 2.5),
  n_steps = 10
)
plot_grid <- visualize_multiscale(sim_data,
                                  Ra_seq = seq(2.5, 20, by = 2.5),
                                  n_steps = 10)
print(plot_grid)
```

---

visualize_sgwt_kernels

Visualize SGWT kernels and scaling functions

Description

Visualize the scaling function and wavelet kernels used in SGWT based on the eigenvalue spectrum and selected parameters

Usage

```
visualize_sgwt_kernels(
  eigenvalues,
  scales = NULL,
  J = 4,
  scaling_factor = 2,
```

```
  kernel_type = "heat",
  lmax = NULL,
  eigenvalue_range = NULL,
  resolution = 1000
)
```

Arguments

eigenvalues	Vector of eigenvalues from graph Laplacian
scales	Vector of scales for the wavelets (if NULL, auto-generated)
J	Number of scales to generate if scales is NULL (default: 4)
scaling_factor	Scaling factor between consecutive scales (default: 2)
kernel_type	Type of wavelet kernel ("mexican_hat" or "meyer", default: "mexican_hat")
lmax	Maximum eigenvalue (optional, computed if NULL)
eigenvalue_range	Range of eigenvalues to plot (default: full range)
resolution	Number of points for smooth curve plotting (default: 1000)

Value

List containing the filter visualization plot and filter values

Examples

```
# Generate some example eigenvalues
eigenvals <- seq(0, 2, length.out = 100)

# Visualize kernels with specific parameters
viz_result <- visualize_sgwt_kernels(
  eigenvalues = eigenvals,
  J = 4,
  scaling_factor = 2,
  kernel_type = "heat"
)
print(viz_result$plot)
```

---

visualize_similarity_xy

Visualize similarity in low vs non-low frequency space

Description

Create a scatter plot with low-frequency similarity (c_low) on x-axis and non-low-frequency similarity (c_nonlow) on y-axis from runSGCC results

Usage

```
visualize_similarity_xy(
  similarity_results,
  point_size = 2,
  point_color = "steelblue",
  add_diagonal = TRUE,
  add_axes_lines = TRUE,
  title = "Low-frequency vs Non-low-frequency Similarity",
  show_labels = FALSE,
  show_names = FALSE
)
```

Arguments

similarity_results	List of similarity results from runSGCC function, or a single result
point_size	Size of points in the plot (default: 2)
point_color	Color of points (default: "steelblue")
add_diagonal	Whether to add diagonal reference lines (default: TRUE)
add_axes_lines	Whether to add x=0 and y=0 reference lines (default: TRUE)
title	Plot title (default: "Low-frequency vs Non-low-frequency Similarity")
show_labels	Whether to show point labels if names are available (default: FALSE)
show_names	Whether to display data point names as text labels using ggrepel (default: FALSE). If more than 50 points, randomly samples 50 for labeling. Requires ggrepel package.

Value

ggplot object showing similarity space visualization

Examples

```
# Create example data and compute SGWT
data <- data.frame(x = runif(100), y = runif(100),
                   signal1 = rnorm(100), signal2 = rnorm(100))
SG <- initSGWT(data, signals = c("signal1", "signal2"))
SG <- runSpecGraph(SG, k = 15)
SG <- runSGWT(SG)

# Single similarity result
sim_result <- runSGCC("signal1", "signal2", SG = SG)
plot <- visualize_similarity_xy(sim_result)
print(plot)

# Multiple similarity results (create two different analyses)
data2 <- data.frame(x = runif(100), y = runif(100),
                    signal1 = rnorm(100), signal2 = rnorm(100))
SG2 <- initSGWT(data2, signals = c("signal1", "signal2"))
```

```
SG2 <- runSpecGraph(SG2, k = 15)
SG2 <- runSGWT(SG2)

sim_results <- list(
  pair1 = runSGCC("signal1", "signal2", SG = SG),
  pair2 = runSGCC("signal1", "signal2", SG = SG2)
)
plot <- visualize_similarity_xy(sim_results, show_names = TRUE)
print(plot)
```

`visualize_stripe_patterns` *Visualize Stripe Pattern Simulation Results*

Description

Create visualization plots for stripe pattern simulation results

Usage

```
visualize_stripe_patterns(
  sim_data,
  gap_seq,
  width_seq,
  theta_seq,
  bg_color = "grey",
  signal1_color = "#1f6f8b",
  signal2_color = "#e67e22",
  overlap_color = "#7a4dbf",
  show_title = TRUE
)
```

Arguments

`sim_data`	Output from simulate_stripe_patterns function
`gap_seq`	Vector of gap values used in simulation
`width_seq`	Vector of width values used in simulation
`theta_seq`	Vector of theta (rotation angle) values used in simulation
`bg_color`	Background color for plots (default: "grey")
`signal1_color`	Color for signal 1 (default: "#1f6f8b")
`signal2_color`	Color for signal 2 (default: "#e67e22")
`overlap_color`	Color for overlapping regions (default: "#7a4dbf")
`show_title`	Logical; if TRUE (default), add titles to plots with parameter values

Value

Combined ggplot object with all pattern visualizations

Examples

```
# Generate and visualize patterns
sim_data <- simulate_stripe_patterns(
  grid_size = 80,
  gap_seq = c(10, 20),
  width_seq = c(5, 10, 20),
  theta_seq = c(0, 30, 60)
)
plot_grid <- visualize_stripe_patterns(sim_data,
                                       gap_seq = c(10, 20),
                                       width_seq = c(5, 10, 20),
                                       theta_seq = c(0, 30, 60))
print(plot_grid)
```

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